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Standard Guide for Estimating the Magnitude of Variability from Expected Sources in Sampling Plans[1]

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1. Scope

1.1 This guide serves as an aid to subcommittees in writing specifications and sampling procedures.

1.2 The guide explains how to estimate the contributions of the variability of lot sampling units, laboratory sampling units, and specimens to the variation of the test result of a sampling plan.

1.3 The guide explains how to combine the estimates of the variability from the three sources to obtain an estimate of the variability of the sampling plan results.

1.4 The guide is applicable to all sampling plans that produce variables data (Note 1). It is not applicable to plans that produce attribute data, since such plans do not take specimens in stages, but require that specimens be taken at random from all of the individual items in the lot.

NOTE 1—This guide is applicable to all sampling plans that produce variables data regardless of the kind of frequency distribution of these data, because no estimates are made of any probabilities.

1.5 This guide includes the following topics:

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2. Referenced Documents

2.1 *ASTM Standards:*

D 123 Terminology Relating to Textiles[2]

D 2904 Practice for Interlaboratory Testing of a Textile Test Method that Produces Normally Distributed Data[2]

D 4271 Practice for Writing Statements on Sampling in Test Methods for Textiles[3]

D 4467 Practice for Interlaboratory Testing of a Textile Test Method that Produces Non-Normally Distributed Data[3]

E 456 Terminology Relating to Quality and Statistics[4]

2.2 ASTM Adjuncts:

TEX-PAC[5]

NOTE 2—Tex-Pac is a group of PC programs on floppy disks, available through ASTM Headquarters, 100 Barr Harbor Drive, Conshohocken, PA 19428, USA. The calculations described in the annexes of this guide, including the cost comparisons of various sampling plans, can be conducted using one of these programs.

3. Terminology

3.1 *Definitions:*

3.1.1 *analysis of variance (ANOVA), n*—a procedure for dividing the total variation of a set of data into two or more parts, one of which estimates the error due to selecting and testing specimens and the other part(s) possible sources of additional variation.

3.1.2 *attribute data, n*—observed values or determinations which indicate the presence or absence of specific characteristics.

3.1.3 *component of variance, n*—a part of a total variance identified with a specific source of variability.

3.1.4 *degrees of freedom, n—for a set*, the number of values that can be assigned arbitrarily and still get the same value for each of one or more statistics calculated from the set of data.

3.1.4.1 *Discussion*— For example, if only an average is specified for a set of five observations, there are four degrees of freedom since the same average can be obtained with any values substituted for four of the observations as long as the fifth value is set to give the correct total. If both the average and standard deviation have been specified, there are only three degrees of freedom left.

3.1.5 *determination value, n*—the numerical quantity calculated by means of the test method equation from the measurement values obtained as directed in a test method. (*Syn.* determination) (See also *observation*.)

3.1.6 *laboratory sample, n*—a portion of material taken to represent the lot sample, or the original material, and used in the laboratory as a source of test specimens.

3.1.7 *lot sample, n*—one or more shipping units taken to represent an acceptance sampling lot and used as a source of laboratory samples.

[1] This guide is under the jurisdiction of ASTM Committee D13 on Textiles and is the direct responsibility of Subcommittee D13.93 on Statistics.

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[2] *Annual Book of ASTM Standards*, Vol 07.01.

[3] *Annual Book of ASTM Standards*, Vol 07.02.

[4] *Annual Book of ASTM Standards*, Vol 14.02.

[5] PC programs on floppy disks are available through ASTM. For a 3½ inch disk request PCN:12-429040-18, for a 5¼ inch disk request PCN:12-429041-18.

3.1.8 *mean square—in analysis of variance*, a contraction of the expression "mean of the squared deviations from the appropriate average(s)" where the divisor of each sum of squares is the appropriate degrees of freedom.

3.1.9 *observation*, *n*—(1) the process of determining the presence or absence of attributes or making measurements of a variable, (2) a result of the process of determining the presence or absence of an attribute or making a measurement of a variable. (Compare *measurement value*, *determination value*, and *test result*.)

3.1.10 *precision*, *n*—the degree of agreement within a set of observations or test results obtained as directed in a method.

3.1.10.1 *Discussion*—The term "precision," delimited in various ways, is used to describe different aspects of precision. This usage was chosen in preference to the use of "repeatability" and "reproducibility" which have been assigned conflicting meanings by various authors and standardizing bodies.

3.1.11 *random sampling*, *n*—the process of selecting units for a sample of size *n* in such a manner that all combinations of *n* units under consideration have an equal or ascertainable chance of being selected as the sample. (*Syn*. simple random sampling and sampling at random.)

3.1.12 *sample*, *n*—(*1*) a portion of a lot of material which is taken for testing or record purposes; (*2*) a group of specimens used, or observations made, which provide information that can be used for making statistical inferences about the population(s) from which they were drawn. (See also *lot sample*, *laboratory sample*, and *specimen*.)

3.1.13 *sampling plan*, *n*—a procedure for obtaining a sample.

3.1.14 *sampling plan result*, *n*—the number obtained for use in judging the acceptability of a lot when applying a sampling plan.

3.1.15 *sampling unit*, *n*—an identifiable, discrete unit or subunit of material that could be taken as part of a sample.

3.1.16 *specimen*, *n*—a specific portion of a material or laboratory sample upon which a test is performed or which is taken for that purpose. (*Syn.* test specimen.)

3.1.17 *sum of squares—in analysis of variance*, a contraction of the expression "sum of the squared deviations from the appropriate average(s)" where the average(s) of interest may be the average(s) of a specific subset(s) of data or of the entire set of data.

3.1.18 *test result*, *n*—a value obtained by applying a test method, expressed either as a single determination or a specified combination of a number of determinations.

3.1.19 *variables data*, *n*—measurements which vary and may take any of a specified set of numerical values.

3.1.20 *variance*, σ^2, *n—of a population*, a measure of the dispersion of members of the population expressed as a function of the sum of the squared deviations from the population mean.

3.1.21 *variance*, s^2, *n—of a sample*, a measure of the dispersion of variates observed in a sample expressed as a function of the squared deviations from the sample average.

3.1.22 For definitions of textile terms, refer to Terminology D 123. For definitions of statistical terms, refer to Terminology D 123 or Terminology E 456, or appropriate textbooks on statistics.

4. Significance and Use

4.1 This guide is useful in estimating the variation due to lot sampling units, laboratory sampling units, and specimen selection and testing during the sampling and testing of a lot of material.

4.2 Estimates of variation from the several sources will make it possible to write sampling plans which balance the cost of sampling and testing with the desired precision of the plan.

4.3 This guide is useful in: (*1*) designing process controls and (*2*) developing sampling plans as parts of product specifications.

4.4 This guide can be used for designing new sampling plans or for improving old plans.

4.5 This guide is concerned with the process of sampling. This is unlike Practice D 2904 or Practice D 4467 which are concerned with the process of testing.

4.6 Studies based on this guide are applicable only to the material(s) on which the studies are made. If the conclusions are to be used for a specification, then separate studies should be made on three or more kinds of materials of the type on which the test method may be used and which produce test results covering the range of interest.

5. Sampling Plans Producing Variables Data

5.1 For the results of using this guide to be completely valid, it is necessary that all of the sampling units at every stage be taken randomly. It is not always practical to achieve complete randomness, but every reasonable effort should be made to do so.

5.2 In sampling plans which produce variables data, there are three stages in which variation can occur. For a schematic representation of these three stages see Fig. 1 (see also Practice D 4271):

5.2.1 *Lot Sample*—Variation among the averages of the sampling units within a lot sample is due to differences between such items as cases, cartons, and bolts, variation among laboratory samples plus test method error and differences among specimens. To estimate variation due to lot sampling units alone, proceed as directed in 5.3 and 5.4.

5.2.2 *Laboratory Sample*—Within the lot sampling units, variation among the averages of the laboratory sampling units is due to differences among such items as cones within cases, garments within cartons, and swatches within bolts, plus test method error and differences among specimens. To estimate variation due to laboratory sampling units alone, proceed as directed in 5.3 and 5.4.

5.2.3 *Specimens*—Variation among determination values on specimens is due to the test method error and the differences among specimens within laboratory sampling units such as cones, garments, and swatches. Usually it is not feasible to separate these two errors. To estimate the variation among specimens proceed as directed in 5.3 and 5.4.

5.3 If a sampling plan has already been put into operation, or if a new plan is proposed, put it into operation, and collect the resulting data. In the case of either an old plan or a new plan, obtain at least two sampling units at each of the stages of